

Package: xtime (via r-universe)

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Type Package

Title Interactive Fixed Effects Estimator for Panel Data

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Description Implements the interactive fixed effects ('IFE') panel estimator of Bai (2009) <[doi:10.3982/ECTA6135](https://doi.org/10.3982/ECTA6135)> with analytical standard errors ('homoskedastic', 'HC1' robust, and cluster-robust by unit). Supports asymptotic bias correction for large panels (Bai 2009) and a dynamic extension for predetermined regressors (Moon and Weidner 2017 <[doi:10.1017/S0266466615000328](https://doi.org/10.1017/S0266466615000328)>). Includes information-criterion-based factor number selection (Bai and Ng 2002 <[doi:10.1111/1468-0262.00273](https://doi.org/10.1111/1468-0262.00273)>). Also implements an unbalanced panel extension using the expectation-maximisation algorithm of Bai (2009) with exact inferential statistics from Su, Wang and Wang (2025) <[doi:10.2139/ssrn.5177283](https://doi.org/10.2139/ssrn.5177283)>, including nuclear-norm regularisation initialisation, singular value thresholding for factor number selection, and analytical bias correction for both strictly and weakly exogenous regressors. All computations use base R only with no external dependencies.

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BugReports <https://github.com/Rickchen0910/xtife/issues>

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cigar	<i>Dataset on US Cigarette Demand Panel</i>
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Description

Balanced panel of cigarette sales and prices across 46 US states for 30 years (1963–1992). Originally used in Baltagi (1995) and widely used as a benchmark dataset for panel estimators.

Usage

cigar

Format

A data frame with 1,380 rows and 9 variables:

state US state identifier (integer, 1–46)

year year (integer, 1963–1992)

price cigarette price index

pop state population

pop16 population aged 16 and over

cpi consumer price index

ndi per-capita disposable income

sales per-capita cigarette sales (packs per person per year)

pimin minimum cigarette price in adjoining states

Source

Baltagi, B.H. (1995) *Econometric Analysis of Panel Data*. Wiley. Distributed with the **plm** R package (Croissant and Millo 2008).

References

Baltagi, B.H. (1995). *Econometric Analysis of Panel Data*. Wiley.

Croissant, Y. and Millo, G. (2008). Panel data econometrics in R: the plm package. *Journal of Statistical Software*, 27(2), 1–43. doi:[10.18637/jss.v027.i02](https://doi.org/10.18637/jss.v027.i02)

ife

*Estimate Interactive Fixed Effects Model (Bai 2009)***Description**

Fits the panel model

$$y_{it} = \alpha_i + \xi_t + X'_{it}\beta + \lambda'_i F_t + u_{it}$$

for balanced panel data with analytical standard errors.

Usage

```
ife(
  formula,
  data,
  index,
  r = 1L,
  force = "two-way",
  se = "standard",
  bias_corr = FALSE,
  method = "static",
  M1 = 1L,
  tol = 1e-09,
  max_iter = 10000L
)
```

Arguments

formula	R formula: outcome ~ covariate1 + covariate2 + ...
data	data.frame in long format (one row per unit-time observation)
index	character(2): c("unit_id_column", "time_id_column")
r	integer >= 0, number of interactive factors (default 1)

force	additive FE specification: "none" "unit" "time" "two-way" (default "two-way"). Additive unit effects α_i and time effects ξ_t are removed via the standard within transformation (iterative demeaning) before the SVD algorithm runs, following Bai (2009) Section 3. Bai (2009, p.1) shows that two-way additive effects are a special case of the interactive structure with $r = 2$ (setting $F_t = (1, \xi_t)'$ and $\lambda_i = (\alpha_i, 1)'$), so the IFE estimator remains consistent when additive effects are present regardless of the force choice, but pre-demeaning improves efficiency.
se	SE type: "standard" "robust" "cluster" (default "standard"; "cluster" clusters by unit id)
bias_corr	logical; if TRUE apply bias correction. For method = "static" uses the two-term Bai (2009) Sec. 7 correction (B/N + C/T). For method = "dynamic" uses the three-term Moon and Weidner (2017) correction (B1/T + B2/N + B3/T). Requires $r > 0$ and at least one covariate. (default FALSE)
method	"static" (default) for Bai (2009) strictly-exogenous regressors; "dynamic" for Moon and Weidner (2017) predetermined regressors (e.g. lagged dependent variable). The dynamic estimator uses double projection $M_\lambda M_F$ on X in the SVD loop.
M1	integer; lag bandwidth for the B1 dynamic bias term (default 1L). Only used when method = "dynamic" and bias_corr = TRUE.
tol	convergence tolerance (default 1e-9)
max_iter	maximum iterations (default 10000L)

Value

An S3 object of class "ife" with the following components:

- coef – named p-vector of estimated coefficients
- vcov – $p \times p$ variance-covariance matrix
- se – named p-vector of standard errors
- tstat – named p-vector of t-statistics
- pval – named p-vector of two-sided p-values
- ci – $p \times 2$ matrix of 95% confidence intervals (CI.lower, CI.upper)
- table – data.frame coefficient table (Estimate, Std.Error, t.value, Pr.t, CI.lower, CI.upper)
- F_hat – $T \times r$ estimated factor matrix
- Lambda_hat – $N \times r$ estimated loading matrix
- residuals – $T \times N$ residual matrix (full model)
- sigma2 – estimated error variance
- df – residual degrees of freedom
- n_iter – iterations to convergence
- converged – logical
- N, T, r, force, se_type – model dimensions and options
- call – matched call

References

- Bai, J. (2009). Panel data models with interactive fixed effects. *Econometrica*, 77(4), 1229–1279. doi:10.3982/ECTA6135
- Moon, H.R. and Weidner, M. (2017). Dynamic linear panel regression models with interactive fixed effects. *Econometric Theory*, 33, 158–195. doi:10.1017/S0266466615000328
- Bai, J. and Ng, S. (2002). Determining the number of factors in approximate factor models. *Econometrica*, 70(1), 191–221. doi:10.1111/14680262.00273

Examples

```
data(cigar, package = "xtife")
fit <- ife(sales ~ price, data = cigar, index = c("state", "year"),
          r = 2, force = "two-way", se = "standard")
print(fit)
```

 ife_select_r

Select the Number of Factors via Information Criteria

Description

Fits the IFE model for $r = 0, 1, \dots, r_max$ and evaluates five information criteria at each value of r . Returns IC1, IC2, and IC3 from Bai and Ng (2002) Proposition 1, applied to IFE residuals per Bai (2009) Section 9.4, plus a BIC-style penalty (IC_bic) and a small-sample-corrected prediction criterion (PC) from Bai (2009). The criterion-minimising r for each IC is flagged with "*" in the printed table, and a data-driven recommendation (favouring IC_bic when the Bai-Ng criteria decrease monotonically) is displayed.

Usage

```
ife_select_r(
  formula,
  data,
  index,
  r_max = NULL,
  force = "two-way",
  verbose = TRUE,
  tol = 1e-09,
  max_iter = 10000L
)
```

Arguments

formula	R formula passed to ife()
data	long-format data.frame
index	character(2): c("unit_id", "time_id")
r_max	maximum r to consider (default: min(8, floor(min(N,T)/2)))

force	additive FE type (default "two-way")
verbose	logical; if TRUE (default) print progress and results table to the console. Set to FALSE for silent operation.
tol	convergence tolerance (default 1e-9)
max_iter	maximum iterations (default 10000L)

Value

(invisibly) a data.frame with columns r, V_r, IC1, IC2, IC3, IC_bic, PC, converged, and attribute "suggested" (named integer vector giving the IC-minimising r for each criterion).

References

Bai, J. (2009). Panel data models with interactive fixed effects. *Econometrica*, 77(4), 1229–1279. doi:10.3982/ECTA6135

Bai, J. and Ng, S. (2002). Determining the number of factors in approximate factor models. *Econometrica*, 70(1), 191–221. doi:10.1111/14680262.00273

Examples

```
data(cigar, package = "xtife")
sel <- ife_select_r(sales ~ price, data = cigar,
                  index = c("state", "year"), r_max = 4)
```

ife_select_r_unb	<i>Factor Number Selection for Unbalanced Panel IFE via SVT</i>
------------------	---

Description

Estimates the number of interactive factors in an unbalanced panel using the singular value thresholding (SVT) rule of Su, Wang and Wang (2025, Section 3.3, eq. 3.7).

Usage

```
ife_select_r_unb(formula, data, index, c_f = 0.6, nu_NT = NULL, verbose = TRUE)
```

Arguments

formula	R formula: outcome ~ covariate1 + covariate2 + ...
data	Data frame in long format.
index	Character vector of length 2: c("unit_col", "time_col").
c_f	SVT threshold constant (default 0.6).
nu_NT	Optional scalar or vector of NNR penalty values. If NULL (default), cross-validates over $c(0.01, 0.1, 1, 10) * \sqrt{\max(N, TT)}$.
verbose	Logical; print result table. Default TRUE.

Value

Invisibly returns a list with components `r_hat`, `sv` (normalised singular values), `threshold`, `c_f`, `c_NT`, and `nu_used`.

References

Su, L., Wang, F. and Wang, Y. (2025). Estimation and inference for unbalanced panel data models with interactive fixed effects. *SSRN Working Paper* 5177283.

Examples

```
data(cigar, package = "xtife")
set.seed(42)
cigar_unb <- cigar[sample(nrow(cigar), 1200L), ]
ife_select_r_unb(sales ~ price, data = cigar_unb,
                 index = c("state", "year"))
```

 ife_unbalanced

Unbalanced Panel Interactive Fixed Effects Estimator

Description

Fits the pure interactive fixed effects model

$$Y_{it} = X'_{it}\beta + \lambda'_i F_t + u_{it}$$

for unbalanced panels (units observed at different sets of time periods) via an Alternating Maximisation (AM) outer loop that iterates between updating $\hat{\beta}$ and the factors $(\hat{\lambda}, \hat{F})$, with the EM algorithm of Bai (2009) Appendix B used as the inner loop to update $(\hat{\lambda}, \hat{F})$ given β . Exact inferential statistics (standard errors and bias correction) follow Su, Wang and Wang (2025).

Usage

```
ife_unbalanced(
  formula,
  data,
  index,
  r = 1L,
  se = "standard",
  init = "ols",
  bias_corr = FALSE,
  exog = "strict",
  L_T = NULL,
  c_f = 0.6,
  nu_NT = NULL,
  tol = 1e-09,
  max_iter = 10000L,
```

```

    tol_em = 1e-07,
    max_iter_em = 500L
)

```

Arguments

formula	R formula: <code>outcome ~ covariate1 + covariate2 + ...</code>
data	Data frame in long format (one row per observed unit-time pair).
index	Character vector of length 2: <code>c("unit_col", "time_col")</code> .
r	Positive integer. Number of interactive factors (default 1). To absorb additive fixed effects into the factor structure (the recommended approach for unbalanced panels; see Description), set <code>r = r_true + 1</code> for unit FE or <code>r = r_true + 2</code> for two-way FE.
se	SE type: "standard" (homoskedastic), "robust" (HC1), "cluster" (cluster-robust by unit), or "hac" (HAC with Bartlett kernel, for serially correlated errors; SWW2025 p.21). Default "standard".
init	Initialisation method: "ols" (default, grand-mean OLS) or "nnr" (nuclear-norm regularisation, SWW2025 Section 3.2).
bias_corr	Logical. Apply the SWW2025 Theorem 4.2 analytical bias correction. Supports both strictly and weakly exogenous regressors (controlled by <code>exog</code>). Default FALSE.
exog	Exogeneity assumption: "strict" (default, regressors uncorrelated with past and future errors) or "weak" (weakly exogenous, e.g., lagged dependent variable $x_{it} = y_{i,t-1}$). When "weak" and <code>bias_corr = TRUE</code> , the additional \hat{b}_2 term from SWW2025 Theorem 4.2 is computed.
L_T	Bartlett kernel bandwidth for HAC standard errors (<code>se = "hac"</code>) and the dynamic bias term \hat{b}_2 (<code>exog = "weak"</code> , <code>bias_corr = TRUE</code>). If NULL (default), set to $\lfloor 2T^{1/5} \rfloor$ after the panel dimensions are known.
c_f	SVT threshold constant (default 0.6, SWW2025 eq. 3.7). Used only when <code>init = "nnr"</code> .
nu_NT	NNR penalty grid. If NULL (default), cross-validates over <code>c * sqrt(max(N, TT))</code> for <code>c</code> in <code>c(0.01, 0.1, 1, 10)</code> .
tol	Outer-loop convergence tolerance on $\max \hat{\beta}^{new} - \hat{\beta}^{old} $. Default <code>1e-9</code> .
max_iter	Maximum outer-loop iterations. Default <code>10000L</code> .
tol_em	Inner EM convergence tolerance. Default <code>1e-7</code> .
max_iter_em	Maximum inner EM iterations per outer step. Default <code>500L</code> .

Details

Additive fixed effects. The SWW2025 model does not include explicit additive unit effects α_i or time effects ξ_t . SWW2025 (p.13, Theorem 3.2 discussion) states that the convergence and asymptotic theory extend "in spirit" to two-way fixed effects models, and (p.17, eq.\ 4.1–4.2 discussion) that "linear/nonlinear panels with one way/two way/interactive fixed effects are all covered by this framework." However, SWW2025 does not formally derive the SE or bias-correction formulas for the explicitly demeaned unbalanced case.

The standard approach — supported by Bai (2009, p.1), who shows that two-way additive effects equal $\lambda_i' F_t$ for the special choice $F_t = (1, \xi_t)'$, $\lambda_i = (\alpha_i, 1)'$ — is to absorb the additive effects into the factor structure by increasing r :

- Unit FE only: set $r = r_true + 1$.
- Two-way FE: set $r = r_true + 2$.

The SWW2025 inferential theory (SE and bias correction) then applies directly to the augmented factor model.

Value

An S3 object of class "ife_unb" with components:

coef Named p-vector of estimated coefficients $\hat{\beta}$ (bias-corrected when `bias_corr = TRUE`).

coef_raw Named p-vector of uncorrected coefficients (only when `bias_corr = TRUE`).

vcov p x p variance-covariance matrix.

se Named p-vector of standard errors.

tstat Named p-vector of t-statistics.

pval Named p-vector of two-sided p-values.

ci p x 2 matrix of 95 percent confidence intervals.

table Data frame coefficient table.

F_hat TT x r estimated factor matrix (normalised $F'F/TT = I_r$).

Lambda_hat N x r estimated loading matrix.

residuals n_obs numeric vector of full-model residuals at observed cells.

sigma2 Estimated error variance ($sum(u^2)/df$).

df Residual degrees of freedom.

n_obs Number of observed unit-time cells.

n_iter Outer-loop iterations to convergence.

converged Logical.

N, TT, r, se_type Model dimensions and options.

init, bias_corr, exog, L_T Options used.

b_hat, b2, b3, b4, b5, b6 Bias components (only when `bias_corr = TRUE`). b2 is a zero vector when `exog = "strict"`.

y_name, x_names, id_col, time_col Variable names.

unit_vals, time_vals Unique unit and time identifiers.

unit_idx, time_idx Integer index vectors for residuals.

call Matched call.

References

- Bai, J. (2009). Panel data models with interactive fixed effects. *Econometrica*, 77(4), 1229–1279. doi:10.3982/ECTA6135
- Su, L., Wang, F. and Wang, Y. (2025). Estimation and inference for unbalanced panel data models with interactive fixed effects. *SSRN Working Paper* 5177283.

Examples

```

data(cigar, package = "xtife")
# Drop ~10 % of rows to create an unbalanced panel
set.seed(1)
cigar_unb <- cigar[sample(nrow(cigar), 1200L), ]
fit <- ife_unbalanced(sales ~ price, data = cigar_unb,
                    index = c("state", "year"), r = 2L)
print(fit)

```

print.ife

Print an IFE Model Summary

Description

Prints a formatted summary of an object of class "ife", including panel dimensions, number of factors, additive fixed effect specification, SE type, and a coefficient table with standard errors, t-statistics, p-values, and 95% confidence intervals. If bias correction was applied, bias terms are also reported. Information criteria are printed when the object contains them (i.e., when called from `ife_select_r()`).

Usage

```

## S3 method for class 'ife'
print(x, digits = 4, ...)

```

Arguments

<code>x</code>	an object of class "ife"
<code>digits</code>	number of significant digits (default 4)
<code>...</code>	unused

Value

`x` invisibly.

Examples

```

data(cigar, package = "xtife")
fit <- ife(sales ~ price, data = cigar, index = c("state", "year"),
          r = 2, force = "two-way", se = "standard")
print(fit)

```

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